



# Performing Meta-Analyses in the Case of Very Few Studies

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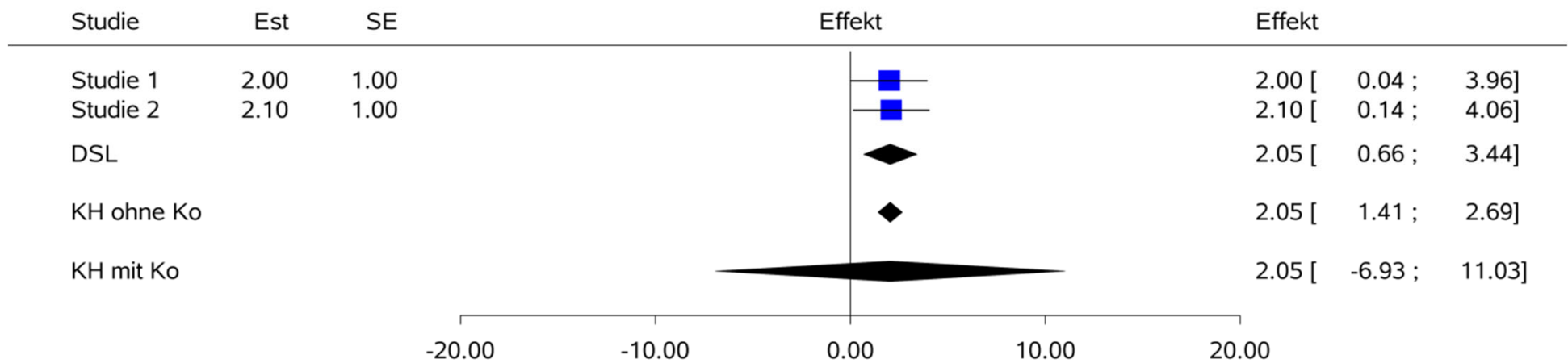
- Introduction
  - Models
  - Estimation methods
  - Qualitative summary of study results
- Meta-analysis with very few studies
  - Problems, examples
  - Qualitative summary of study results
  - Procedure, examples
- Discussion
- Outlook
  - Beta-binomial Model
  - Bayesian meta-analysis
- Summary
- Conclusion
- References

Poll 1: Continent

Poll 2: Affiliation

# Topic for today:

## Meta-analyses with very few studies



tau<sup>2</sup> PM: 0.000

### Methods for evidence synthesis in the case of very few studies

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Guido Schwarzer<sup>6</sup> | Guido Skipka<sup>1</sup>

*Res Syn Meth.* 2018;**9**:382–392.

### Performing Meta-analyses with Very Few Studies

Anke Schulz, Christoph Schürmann, Guido Skipka, and Ralf Bender

In: Evangelou, E. & Veroniki, A.A., Eds.: *Meta-Research: Methods and Protocols*, pp. 91-102. Humana, New York (2022)

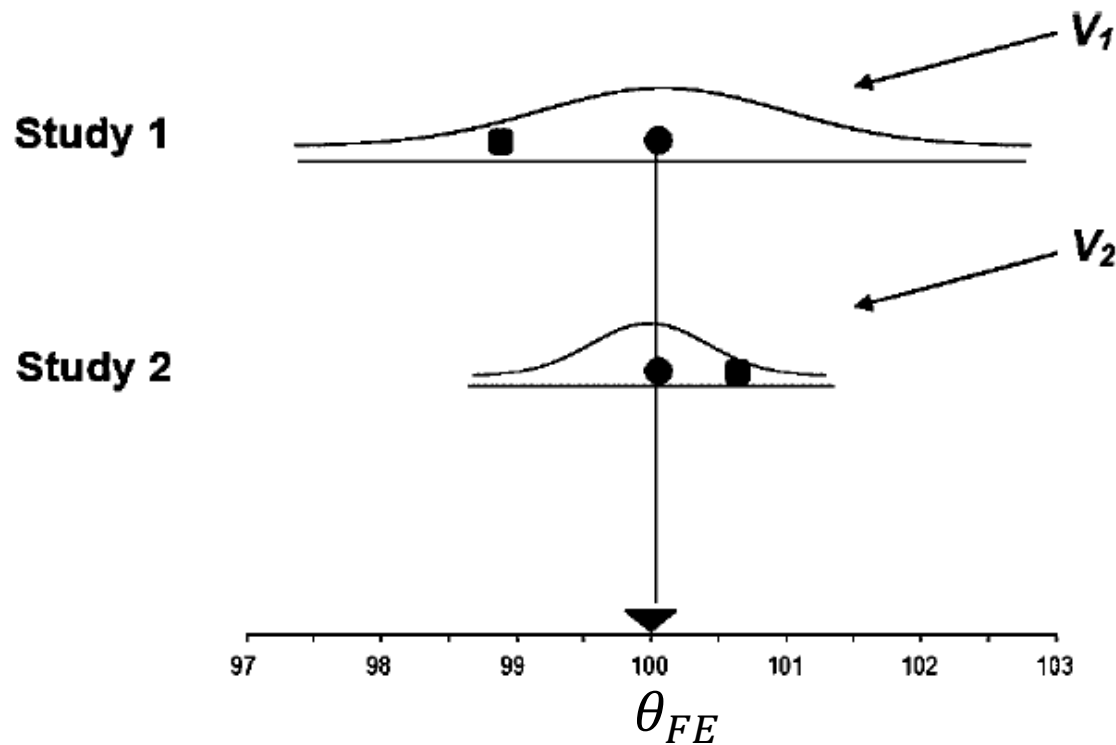
2 main meta-analytic models:

- Model with fixed effect (FEM)
  - Assumption:  
All studies estimate the same effect
  - Better term: "*Common-effect model*"
  
- Model with random effects (REM)
  - Assumption:  
The studies estimate different effects
  - For illustrating heterogeneity:  
**Prediction intervals (PIs)** are useful

Note: There are more models and approaches for meta-analysis. However, in practice, these do not play a major role (see Bender et al., *RSM* 2018).

# Meta-analysis: FEM

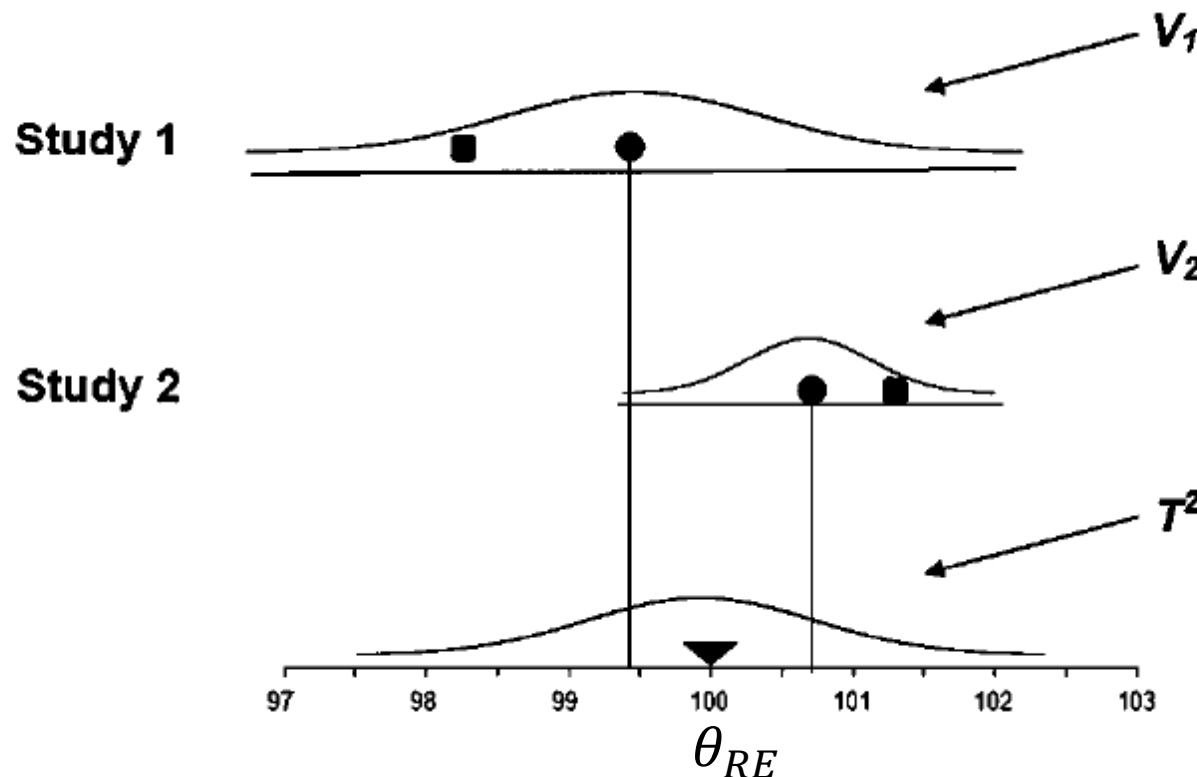
- $y_i = \theta_{FE} + \varepsilon_i$  ,  $\varepsilon_i \sim N(0, v_i)$  ,  $Var(y_i) = v_i$
- Assumption: All studies estimate the same effect.
- Parameter of interest: **Fixed effect  $\theta_{FE}$**



From: Borenstein et al. (2010): *RSM* 1, 97-111.

# Meta-analysis: REM

- $y_i = \theta_i + \varepsilon_i$ ,  $\theta_i = \theta_{RE} + \delta_i$ ,  $\varepsilon_i \sim N(0, v_i)$ ,  $\delta_i \sim N(0, \tau^2)$ ,  $Var(y_i) = v_i + \tau^2$
- Assumption: Each study estimates a study-specific true effect.
- Parameter of interest: **Expected value  $\theta_{RE}$  of the effects**



From: Borenstein et al. (2010): *RSM* 1, 97-111.

- Confidence interval (CI):

- 95%-CI:  $\hat{\theta}_{RE} \pm t_{k-1, 1-\frac{\alpha}{2}} \times SE(\hat{\theta}_{RE})$

- Range, which includes with high certainty (95%) the true effect of the meta-analysis

- Prediction interval (PI):

- 95%-PI:  $\hat{\theta}_{RE} \pm t_{k-1, 1-\frac{\alpha}{2}} \times \sqrt{\tau^2 + Var(\hat{\theta}_{RE})}$

- Range, which includes with high certainty (95%) the true effect of a single study

- Graphical illustration of heterogeneity in the REM

## FEM: Inverse variance (IV)

- Continuous data: Method of inverse variance (IV)
- Point estimate:  $\hat{\theta}_{FE} = \frac{\sum_{i=1}^k y_i w_{i,FE}}{\sum_{i=1}^k w_{i,FE}}$ , with  $w_{i,FE} = 1/\hat{v}_i$
- 95% CI:  $\hat{\theta}_{FE} \pm z_{1-\frac{\alpha}{2}} \sqrt{\frac{1}{\sum_{i=1}^k w_{i,FE}}}$ ,  $z_q$ :  $q$ -quantile of the normal distribution

## FEM: Mantel-Haenszel (MH)

- Binary data: Mantel-Haenszel (MH) method
- Estimation performed by means of the fourfold tables (dependent on effect measure)



## REM: DerSimonian & Laird (DSL)

- Historically, the standard approach for RE meta-analysis: DSL method (DerSimonian & Laird, *CCT* 1986)
- Point estimation:  $\hat{\theta}_{RE} = \frac{\sum_{i=1}^k y_i w_{i,RE}}{\sum_{i=1}^k w_{i,RE}}$  with  $w_{i,RE} = 1/(\hat{v}_i + \hat{\tau}^2)$
- Point estimation of  $\tau$  by means of the method of moments
- 95% CI:  $\hat{\theta}_{RE} \pm z_{1-\frac{\alpha}{2}} \sqrt{\frac{1}{\sum_{i=1}^k w_{i,RE}}}$ ,  $z_q$ :  $q$ -quantile of normal distribution
- DSL has been criticized for some time (Cornell et al., *AIM* 2014)
- DSL ignores the uncertainty of variance estimations
- CIs are frequently too narrow (in the case of few studies)

## REM: Hartung-Knapp-Sidik-Jonkman (HKSJ)

- Recommended by the Cochrane Collaboration: HKSJ method (Veroniki et al., *RSM* 2019)
- Estimation:  $\hat{\theta}_{RE} = \frac{\sum_{i=1}^k y_i w_{i,RE}}{\sum_{i=1}^k w_{i,RE}}$  with  $w_{i,RE} = 1/(\hat{v}_i + \hat{\tau}^2)$
- Estimation of  $\tau$  by means of Paule-Mandel method
- 95% CI:  $\hat{\theta}_{RE} \pm t_{k-1, 1-\frac{\alpha}{2}} \sqrt{\frac{\sum_{i=1}^k w_{i,RE} (y_i - \hat{\theta}_{RE})^2}{(k-1) \sum_{i=1}^k w_{i,RE}}}$ ,  $t_{m,q}$ : q-quantile of t-distribution
- HKSJ holds type 1 error
- CIs frequently very wide (especially in the case of few studies)
- $z_{0.975} = \mathbf{1.96}$ ,  $t_{1;0.975} = \mathbf{12.7}$ ,  $t_{2;0.975} = \mathbf{4.3}$ ,  $t_{3;0.975} = \mathbf{3.2}$ ,  $t_{4;0.975} = \mathbf{2.8}$

## REM: Hartung-Knapp-Sidik-Jonkman (HKSJ)

- Problems in homogeneous data situations

- 95% CI:  $\hat{\theta}_{RE} \pm t_{k-1, 1-\frac{\alpha}{2}} \sqrt{\frac{\sum_{i=1}^k w_{i,RE} (y_i - \hat{\theta}_{RE})^2}{(k-1) \sum_{i=1}^k w_{i,RE}}}$

- SE may be arbitrarily too small and CI too narrow
- Ad-hoc variance correction (Knapp & Hartung, *Stat. Med.* 2003)

- $Var(\hat{\theta}_{RE}) = \max \left[ \frac{1}{\sum_{i=1}^k w_{i,RE}}, \frac{\sum_{i=1}^k w_{i,RE} (y_i - \hat{\theta}_{RE})^2}{(k-1) \sum_{i=1}^k w_{i,RE}} \right]$

- Procedure required for the decision whether the ad-hoc variance correction (VC) should be used or not

## Concept of conclusive effects (IQWiG, 2022):

- Data situation, in which an effect can be derived although a meaningful pooled effect estimation is not possible
- No pooled effect estimation when:
  - Heterogeneity is too large
  - Data are insufficient to apply the desired model (REM)

## Concept of conclusive effects (IQWiG, 2022):

- 2 or more estimates are in the same direction
  - Total weight of these studies  $\geq 80\%$
  - $\geq 2$  studies are statistically significant
  - Weight of significant studies  $\geq 50\%$
- Moderately and clearly conclusive effects
  - 2 or 3 studies significant  $\Rightarrow$  clearly
  - 2 studies significant, 1 study n.s.  $\Rightarrow$  moderately
  - Conclusive situation with 4 studies:
    - all 4 studies significant  $\Rightarrow$  clearly
    - Null  $\notin$  prediction interval  $\Rightarrow$  clearly
    - Null  $\in$  prediction interval  $\Rightarrow$  moderately

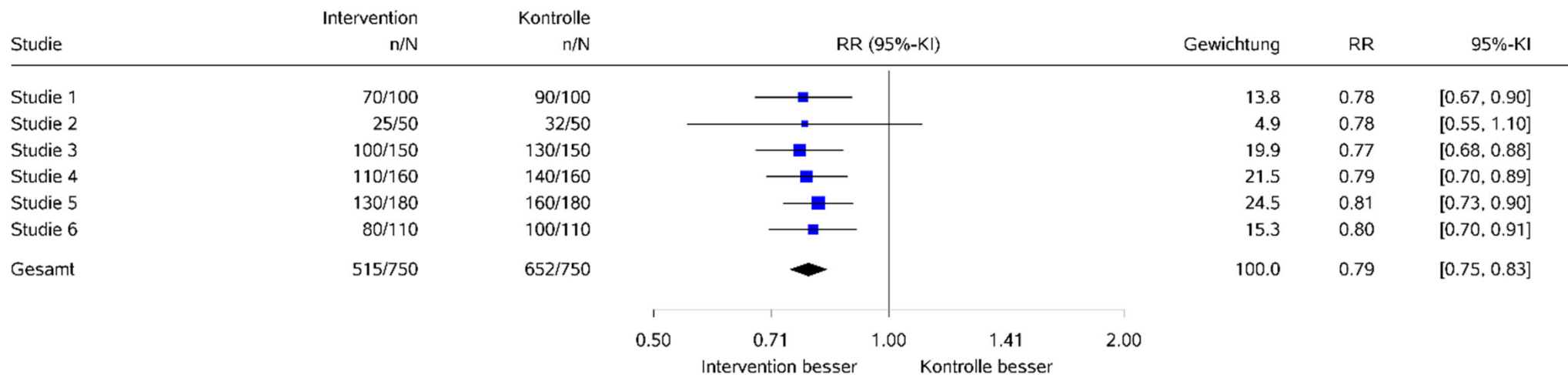
# General examples

## Example 1: Clear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit festem Effekt - Mantel-Haenszel



Heterogenität:  $Q=0.54$ ,  $df=5$ ,  $p=0.991$ ,  $I^2=0\%$

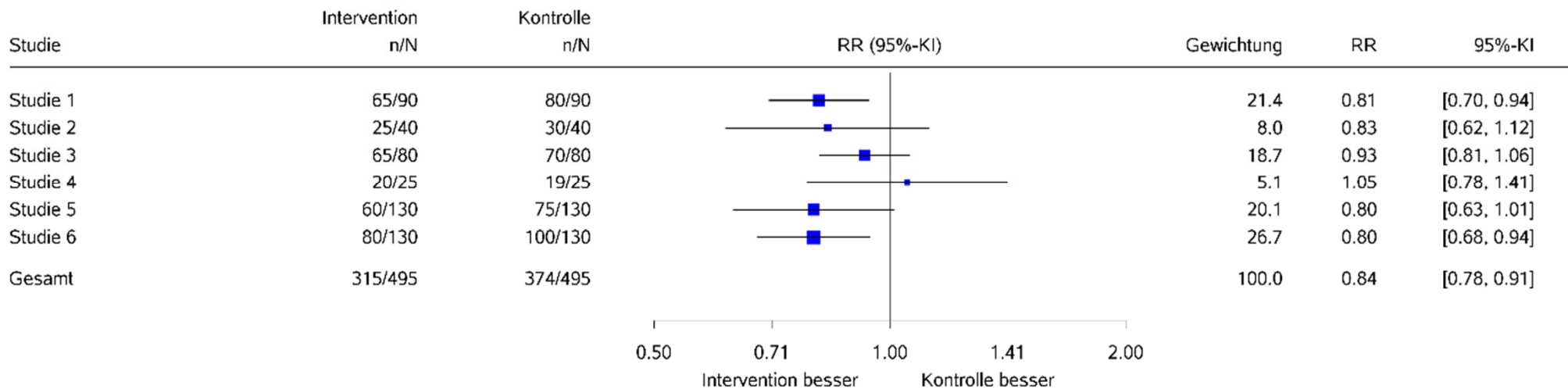
Gesamteffekt:  $Z\text{-Score}=-8.37$ ,  $p<0.001$

⇒ Proof of an intervention effect

# General examples

## Example 2: Less clear data situation

Intervention vs. Kontrolle  
 Endpunkt X  
 Modell mit festem Effekt - Mantel-Haenszel



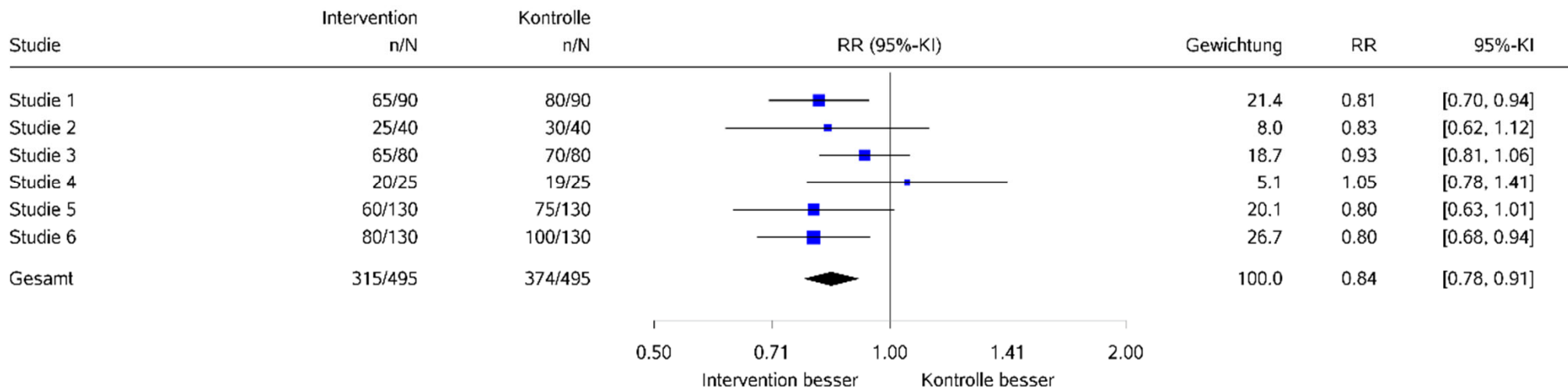
Heterogenität:  $Q=5.02$ ,  $df=5$ ,  $p=0.413$ ,  $I^2=0.4\%$   
 Gesamteffekt: Z-Score=-4.17,  $p<0.001$

Poll 3: Significant effect?

# General examples

## Example 2: Less clear data situation

Intervention vs. Kontrolle  
 Endpunkt X  
 Modell mit festem Effekt - Mantel-Haenszel



Heterogenität:  $Q=5.02$ ,  $df=5$ ,  $p=0.413$ ,  $I^2=0.4\%$   
 Gesamteffekt:  $Z\text{-Score}=-4.17$ ,  $p<0.001$

⇒ Proof of an intervention effect



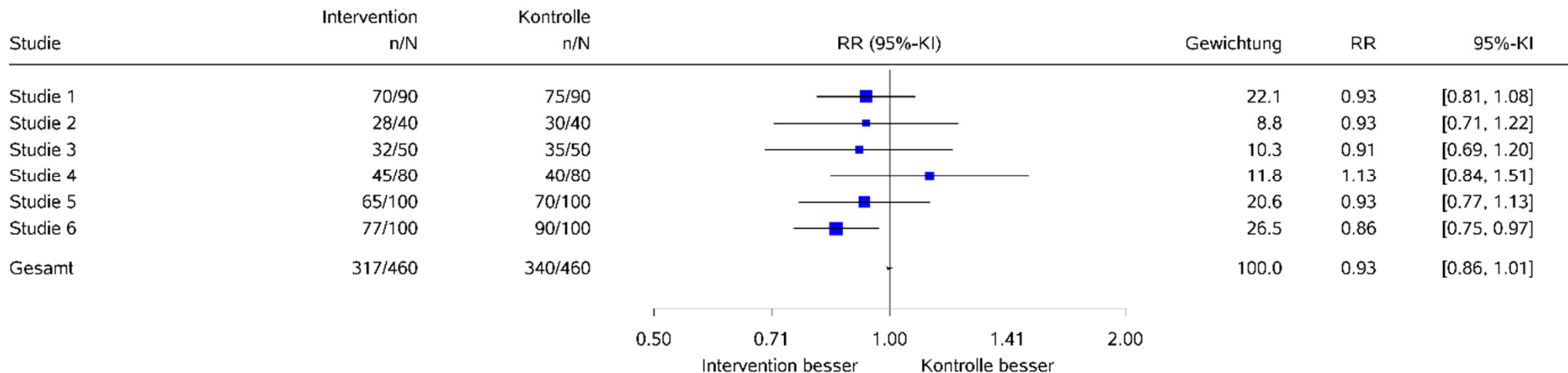
# General examples

## Example 3: Unclear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit festem Effekt - Mantel-Haenszel



Heterogenität:  $Q=3.41$ ,  $df=5$ ,  $p=0.637$ ,  $I^2=0\%$

Gesamteffekt:  $Z\text{-Score}=-1.72$ ,  $p=0.086$

## Poll 4: Significant effect?

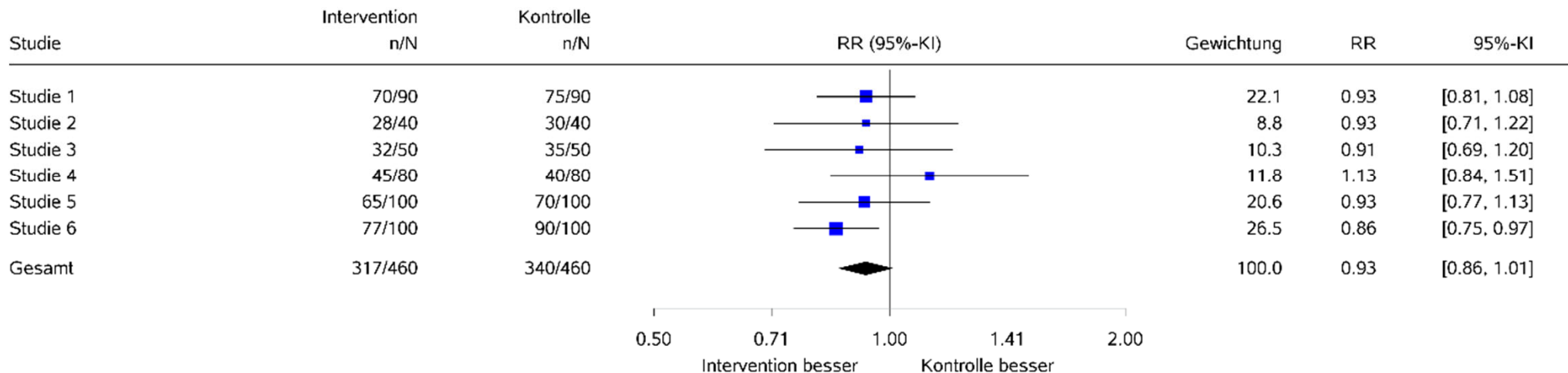
# General examples

## Example 3: Unclear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit festem Effekt - Mantel-Haenszel



Heterogenität:  $Q=3.41$ ,  $df=5$ ,  $p=0.637$ ,  $I^2=0\%$

Gesamteffekt:  $Z\text{-Score}=-1.72$ ,  $p=0.086$

⇒ No proof of an intervention effect

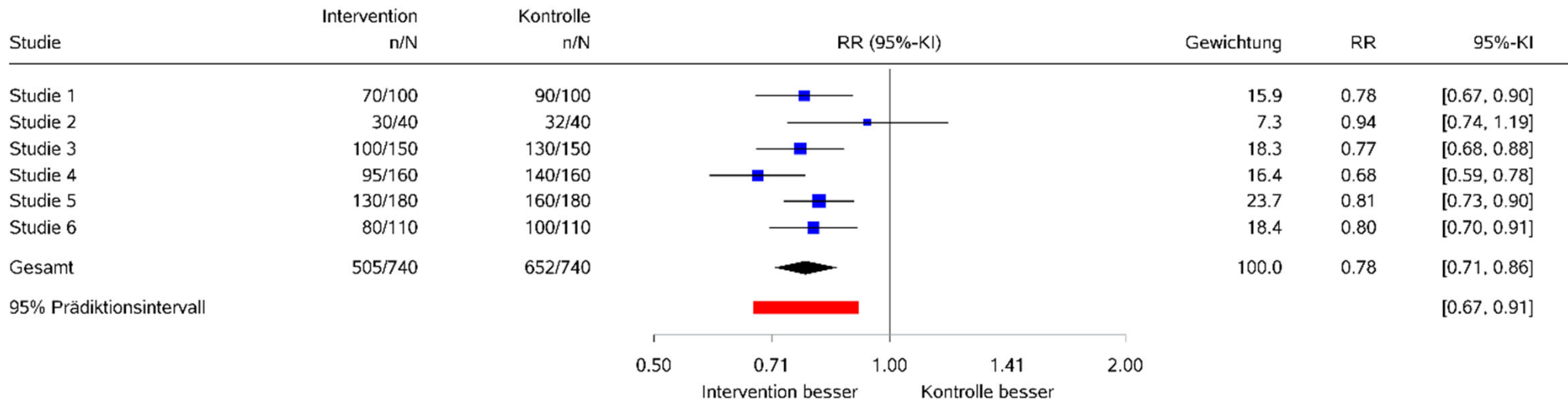
# General examples

## Example 4: REM in clear data situation

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung



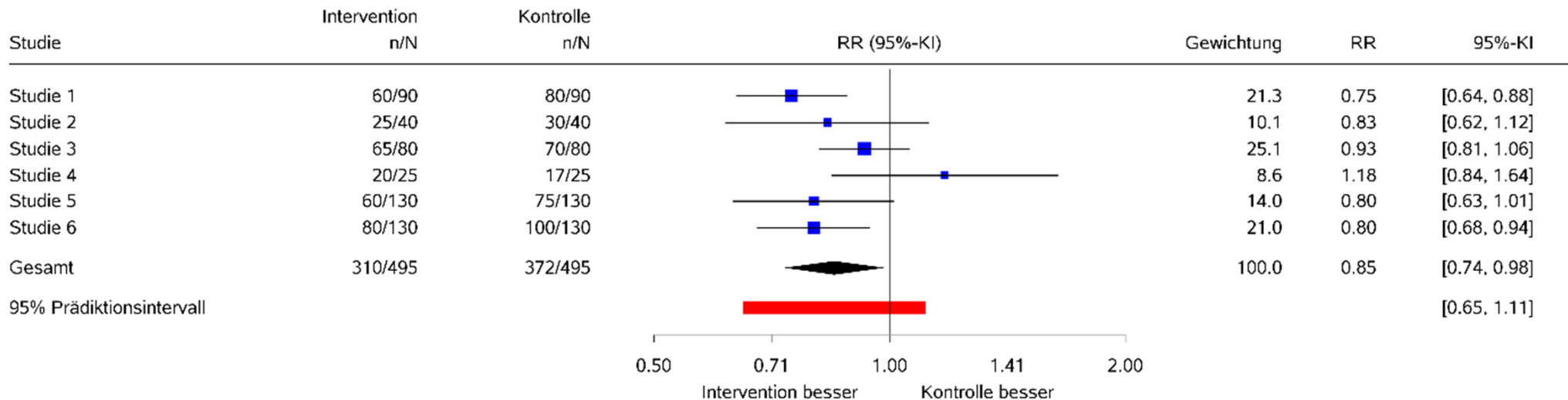
Heterogenität:  $Q=6.95$ ,  $df=5$ ,  $p=0.224$ ,  $I^2=28.1\%$

Gesamteffekt:  $Z\text{-Score}=-7.01$ ,  $p<0.001$ ,  $\text{Tau(Paule-Mandel)}=0.049$

⇒ Proof of an intervention effect

## Example 5: REM in less clear data situation

Intervention vs. Kontrolle  
 Endpunkt X  
 Modell mit zufälligen Effekten - Knapp und Hartung



Heterogenität:  $Q=8.58$ ,  $df=5$ ,  $p=0.127$ ,  $I^2=41.7\%$   
 Gesamteffekt:  $Z\text{-Score}=-2.90$ ,  $p=0.034$ ,  $\text{Tau(Paule-Mandel)}=0.088$

Provided there is sufficient certainty of the study results, the pooled effect estimate indicates **proof of an intervention effect** (on average!).  
 However, due to heterogeneity, study situations can be expected, in which the intervention has no effect.

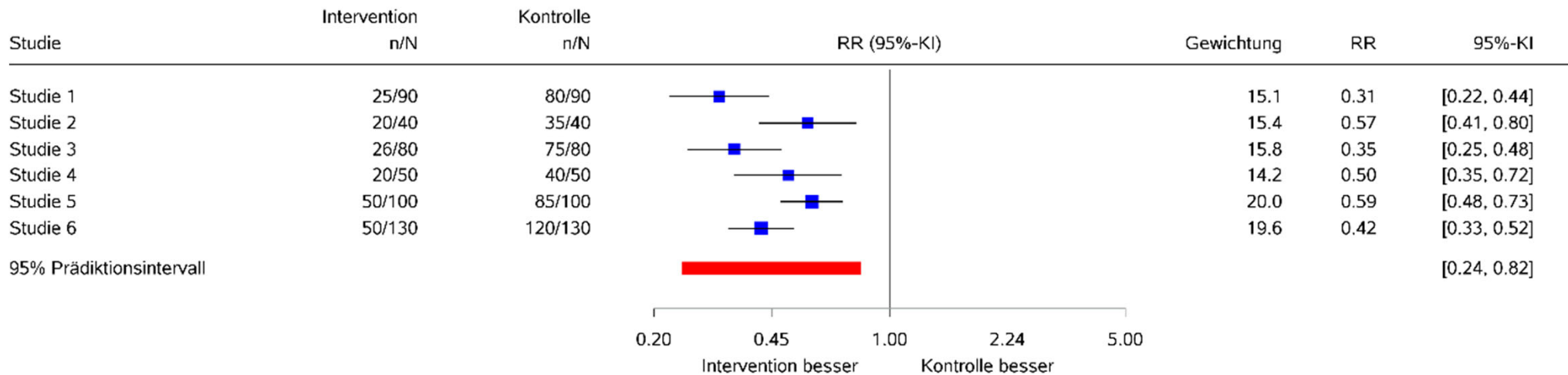
# General examples

## Example 6: Clearly conclusive effects

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung (zur Darstellung der Gewichte)



Heterogenität:  $Q=16.30$ ,  $df=5$ ,  $p=0.006$ ,  $I^2=69.3\%$

Provided there is sufficient certainty of the study results, the clearly conclusive effects indicate **proof of an intervention effect** (but with an unclear effect size).

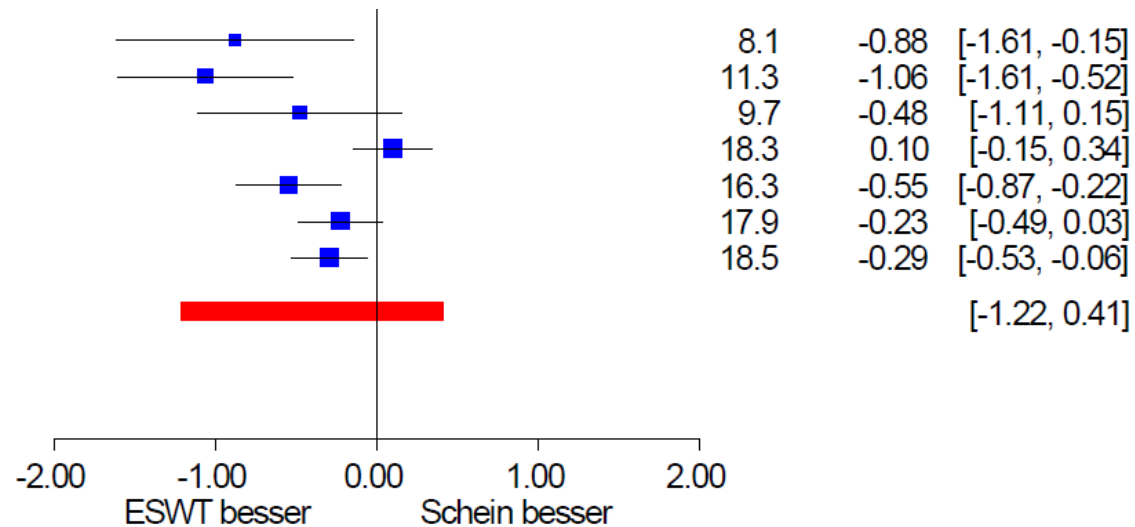
# General examples

## Example 7: Moderately conclusive effects

Abt 2002	17	1.40	2.21	15	3.40	2.21
Cosentino 2001	30	4.00	3.89	30	8.20	3.89
Gollwitzer 2007	20	-4.50	5.13	20	-2.00	5.13
Haake 2003	129	5.20	3.10	131	4.90	3.10
Malay 2006	112	-3.39	2.93	56	-1.78	2.93
Ogden 2001	118	3.48	3.11	114	4.18	3.04
Ogden 2004	144	3.43	2.90	141	4.28	2.90

95% Prädiktionsintervall

Heterogenität:  $Q=22.95$ ,  $df=6$ ,  $p<0.001$ ,  $I^2=73.9\%$



The decision, whether the intervention is beneficial depends on the certainty of the study results.

(RCTs with low risk of bias or non-RCTs with high or unclear risk of bias?)

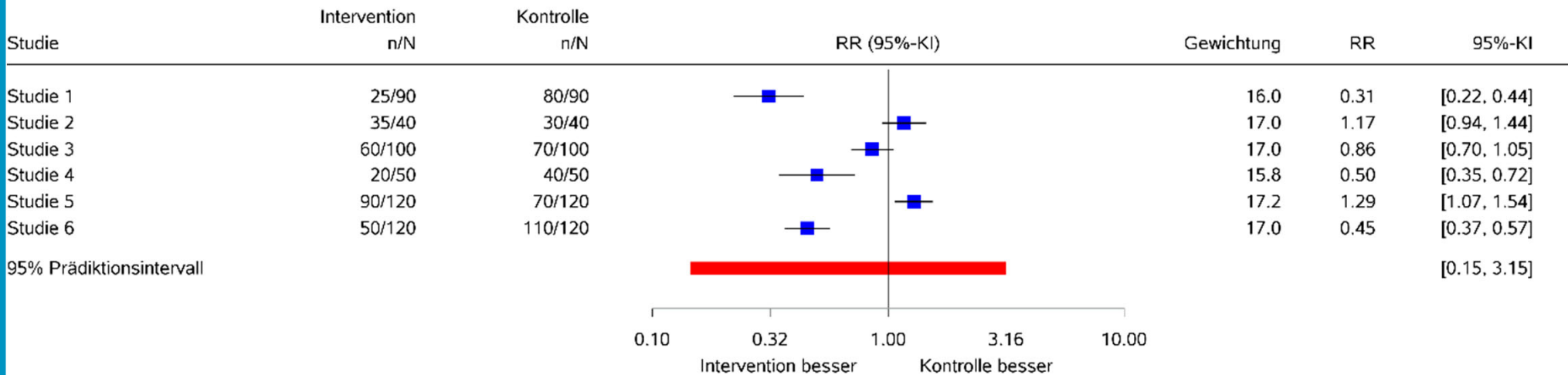
# General examples

## Example 8: No conclusive effects

Intervention vs. Kontrolle

Endpunkt X

Modell mit zufälligen Effekten - Knapp und Hartung (zur Darstellung der Gewichte)



Heterogenität:  $Q=107.73$ ,  $df=5$ ,  $p<0.001$ ,  $I^2=95.4\%$

⇒ No proof of an intervention effect

# Very few studies ( $k < 5$ )

Problems with meta-analyses with very few studies (Bender et al., 2018):

- Choice between FEM and REM difficult
- $\tau$  cannot be adequately estimated
- DSL-CIs are too narrow
- HKSJ-CIs are wide or even non-informative
- In homogeneous data situations HKSJ-CIs are sometimes too narrow

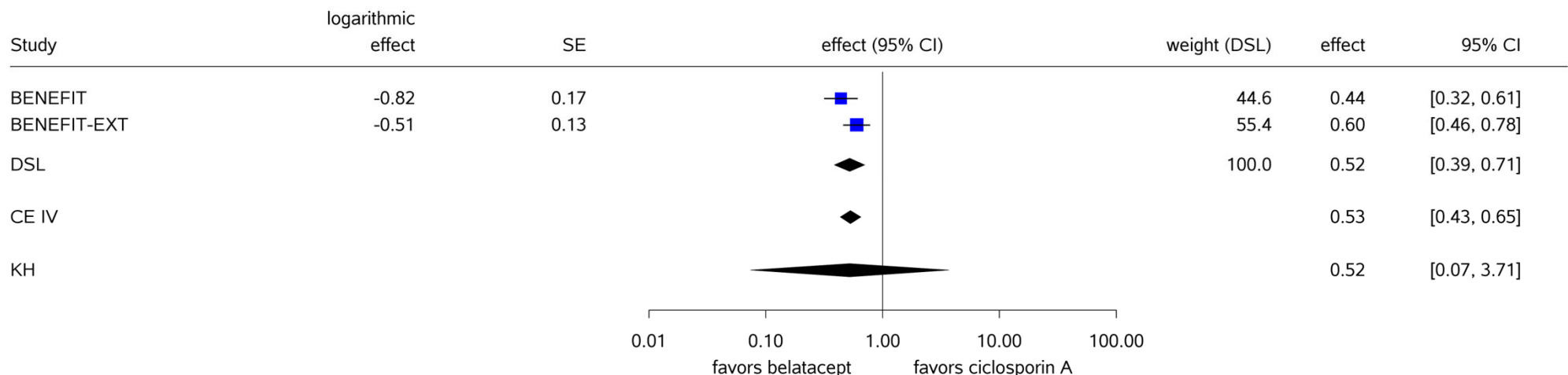


# Example: IQWiG Report A15-25

## Belatacept after kidney transplant (2 significant studies)

- Belatacept vs ciclosporin A for prophylaxis of graft rejection in adults receiving a renal transplant
- Endpoint "renal insufficiency in chronic kidney disease stage 4/5"

belatacept vs. ciclosporin A  
renal insufficiency in chronic kidney disease



Heterogeneity:  $Q=2.06$ ,  $df=1$ ,  $p=0.151$ ,  $I^2=51.5\%$   
Overall effect: Z Score=-4.21,  $p<0.001$ , Tau=0.157

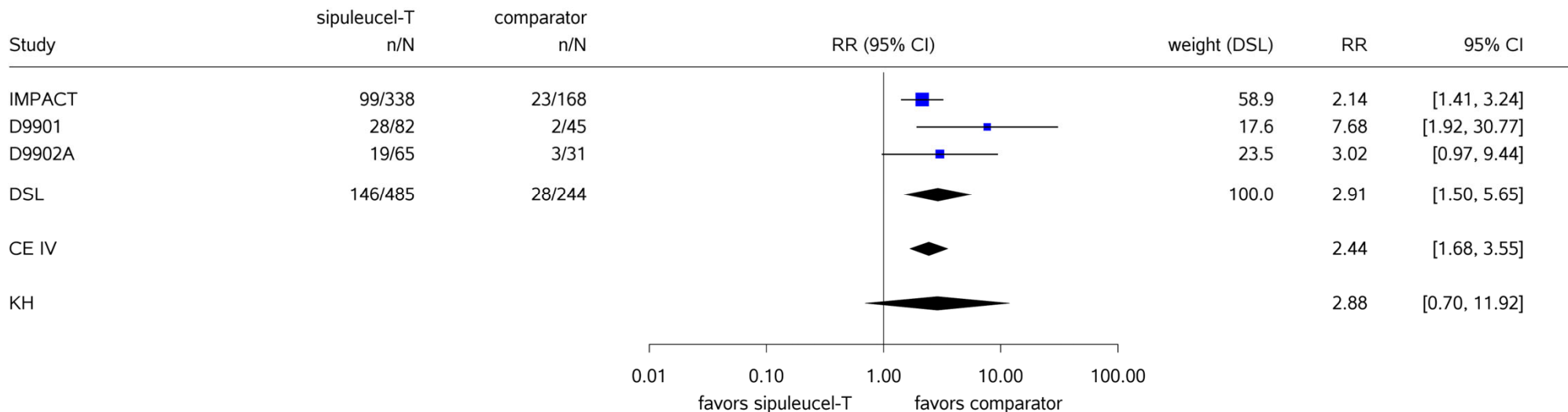


- 1) HKSJ over-conservative
- 2) Decision of no added benefit would be critical

## Sipuleucel-T in prostate cancer (3 significant studies)

- Sipuleucel-T vs appropriate comparator for asymptomatic or minimally symptomatic metastatic prostate cancer in males
- Endpoint fever

sipuleucel-T vs. comparator  
fever

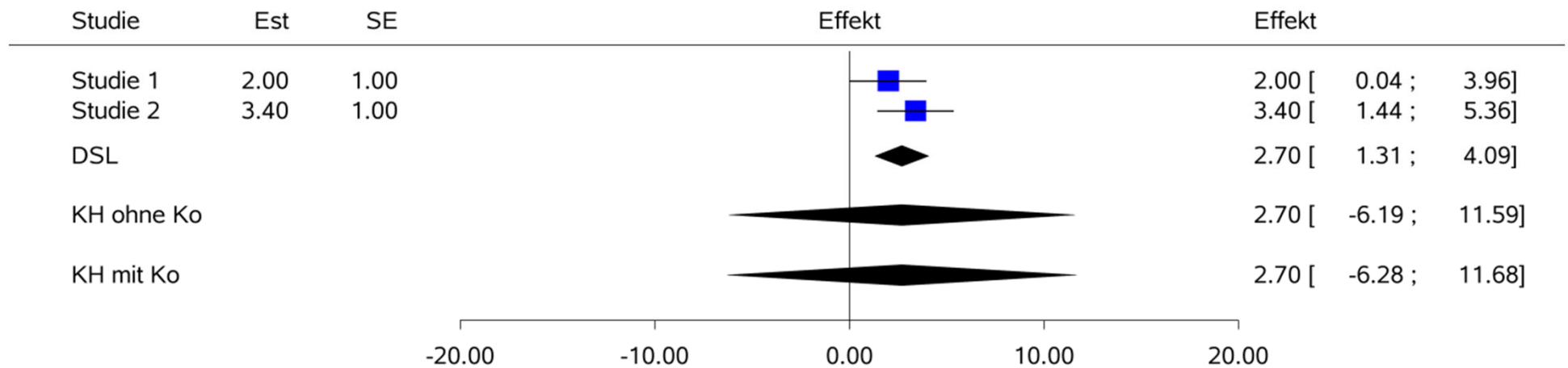


Heterogeneity:  $Q=3.29$ ,  $df=2$ ,  $p=0.193$ ,  $I^2=39.1\%$   
Overall effect: Z Score=3.15,  $p=0.002$ , Tau=0.388

→ **Even in the case of 3 studies HKSJ method over-conservative**

# Artificial examples

## Ad-hoc variance correction (VC) for HKSJ



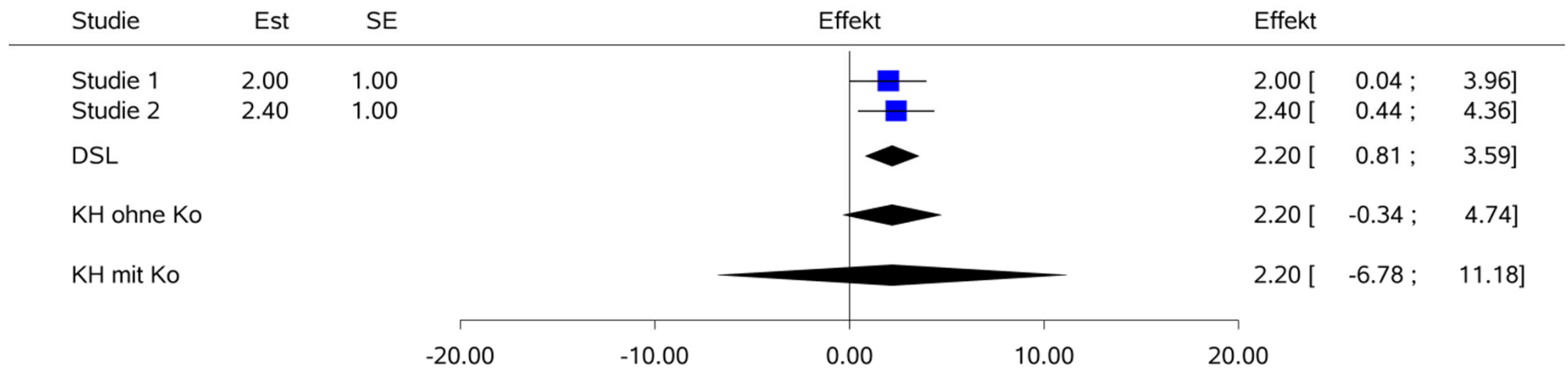
tau<sup>2</sup> PM: 0.000



HKSJ over-conservative  
Ad-hoc VC not required

# Artificial examples

## Ad-hoc variance correction (VC) for HKSJ



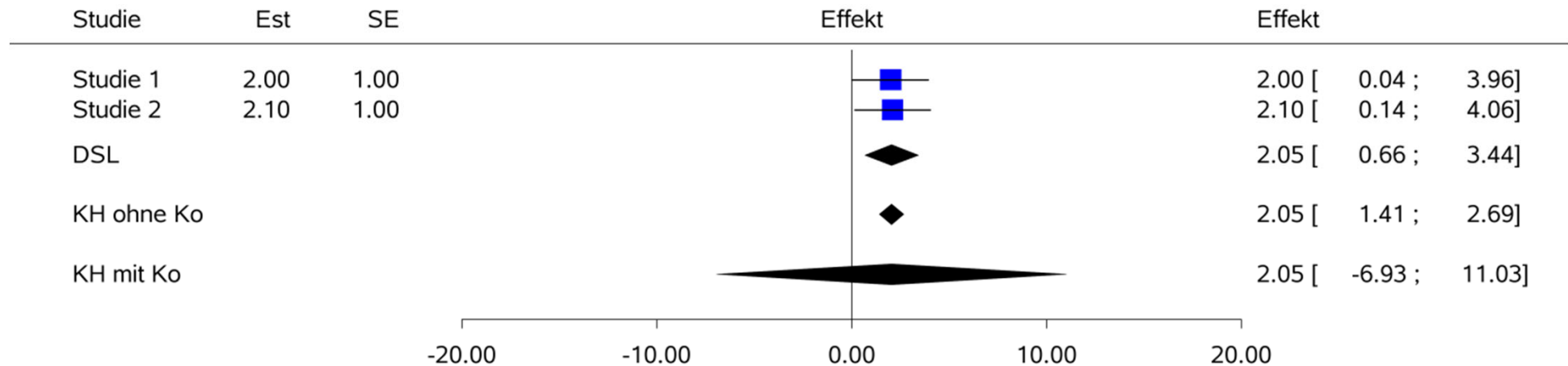
tau<sup>2</sup> PM: 0.000



HKSJ CI-width decreases with increasing homogeneity  
Is the use of ad-hoc VC required?

# Artificial examples

## Ad-hoc variance correction (VC) for HKSJ



HKSJ-CI clearly too narrow  
Variance correction required, but over-conservative



Comparison with DSL to decide whether  
ad-hoc VC should be used (Schulz et al., 2022)

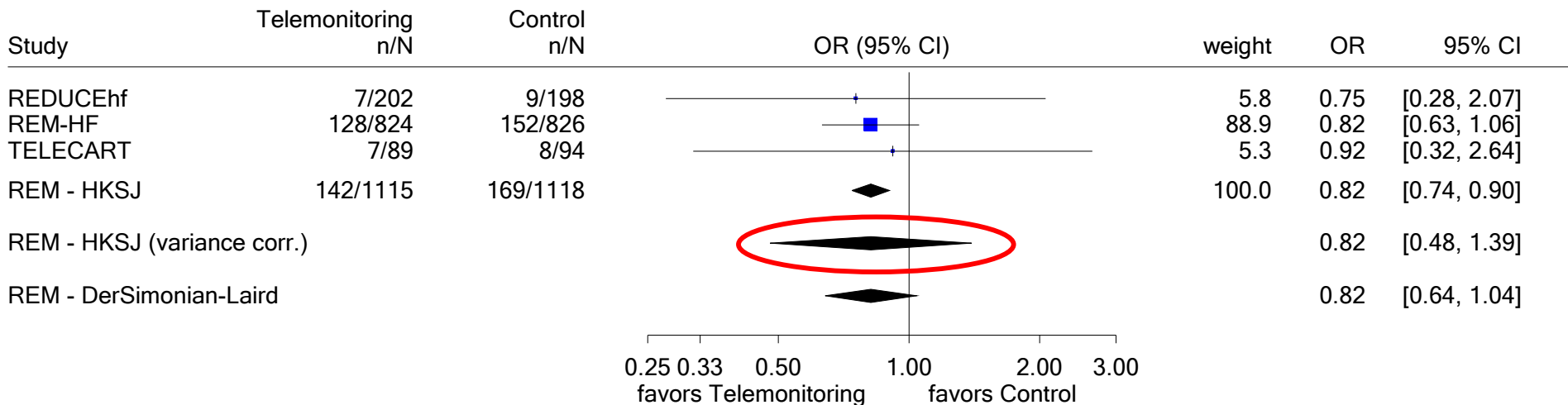
# Procedure in the case of very few studies IQWiG

- Step 1: Preliminary model choice
  - PICOS framework
  - In general: RE model
  - 2 studies: FE model (studies with identical design)
- Step 2: Evaluation of heterogeneity
  - Too large, unexplained heterogeneity: MA not useful
  - Q-Test,  $I^2$ , visual inspection of forest plot
  - If this is the case: Qualitative summary (QS)
- Step 3: Final model and method choice
  - Strong heterogeneity: Reconsider preliminary choice
  - FE model: IV (continuous) or MH (binary)
  - RE model: HKSJ (if required VC) or QS  
(comparison with DSL and comparison with QS)

# Example: IQWiG Report N16-02

- Use of ad-hoc VC required?
  - Comparison of CIs from DSL and HKSJ
  - HKSJ-CI narrower than DSL-CI  $\Rightarrow$  Use VC

Telemonitoring vs. Control  
Mortality



Heterogeneity:  $Q=0.07$ ,  $df=2$ ,  $p=0.965$ ,  $I^2=0\%$   
 Overall effect (REM - HKSJ):  $Z$  Score=-8.66,  $p=0.013$ ,  $\text{Tau(Paule-Mandel)}=0$

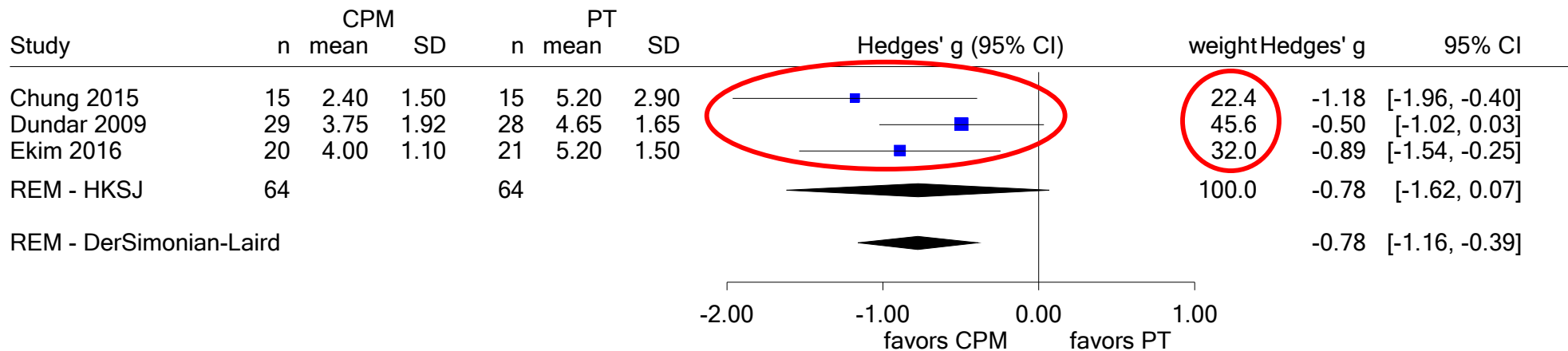


HKSJ (VC)  $\Rightarrow$  No proof of an effect

# Example: IQWiG Report N16-03

- Is HKSJ informative? Significance of HKSJ vs DSL?
  - HKSJ-CI wider than the union of study CIs?
  - HKSJ informative, but n.s., DSL stat. sign.  $\Rightarrow$  QS

Continuous Passive Motion vs. Physical Therapy  
Pain



Heterogeneity:  $Q=2.23$ ,  $df=2$ ,  $p=0.328$ ,  $I^2=10.2\%$   
Overall effect (REM - HKSJ): Z Score=-3.96,  $p=0.058$ , Tau(Paule-Mandel)=0.107

→

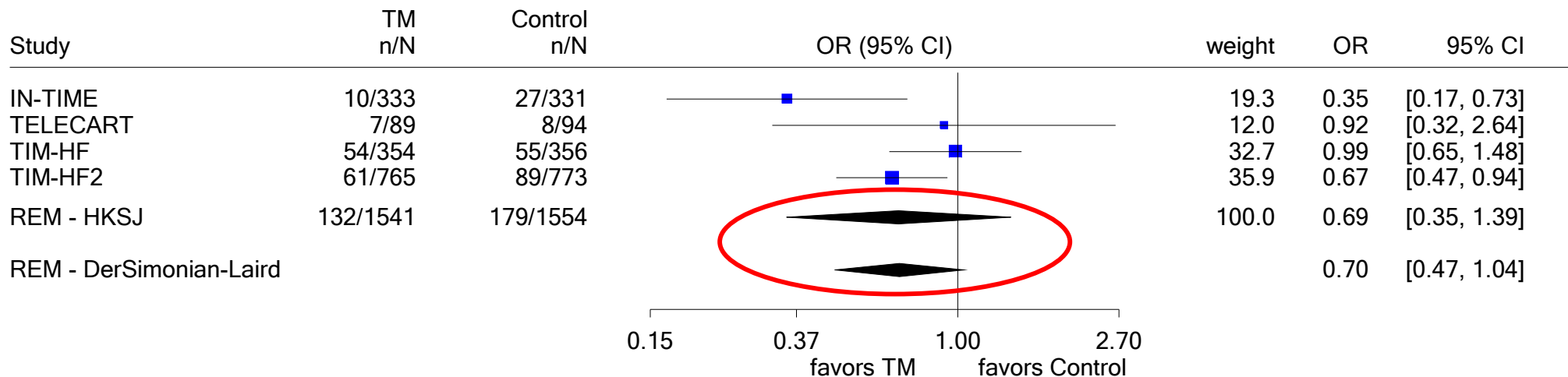
QS  $\Rightarrow$  Benefit of the intervention  
 (but effect size is unclear)



# Example: IQWiG Report N19-01

- Is HKSJ informative? Significance of HKSJ vs DSL?
  - HKSJ-CI wider than the union of study CIs?
  - HKSJ informative, but n.s., DSL n.s.  $\Rightarrow$  HKSJ & DSL

Telemedicine vs. Control  
Mortality



Heterogeneity:  $Q=6.34$ ,  $df=3$ ,  $p=0.096$ ,  $I^2=52.7\%$   
Overall effect (REM - HKSJ): Z Score=-1.68,  $p=0.192$ , Tau(Paule-Mandel)=0.318



**HKSJ & DSL  $\Rightarrow$  No proof of an effect**

- No satisfactory standard method is currently available to perform meta-analyses in the case of very few studies
- FEM possible in practice, but has limitations
- **Therefore, in general, the REM should be used** (unless there are clear reasons to justify the use of the FEM)
- Problem: In the case of very few studies, REM frequently has low power and does not yield informative results
- **In the case of only 2 studies, the FEM should be used** (despite of the general recommendation) unless there are clear reasons against the use of the FEM
- Reason: In situations with only 1 single study, results of this study are interpreted and conclusions are made (in principle, application of the FEM)

- In the case of **3-4 studies**: **REM** should be used (unless there are clear reasons to justify the use of the FEM)
- Use of HKSJ (with checks regarding VC and whether the result is informative)
- Application of **HKSJ** or **HKSJ-VC** or **QS**
- For QS:
  - Concept of conclusive effects
  - Prediction intervals
- Other promising possibilities:
  - Beta-binomial model  
(Felsch et al., *BMC-MRM* 2022)
  - Bayesian meta-analysis with informative prior for  $\tau$   
(Röver et al., *RSM* 2021; Lilienthal et al., work in progress)

## Beta-binomial model (BBM)

- Suitable for binary data
- Simulation study by IQWiG in collaboration with Tim Mathes (Göttingen) and Oliver Kuß (Düsseldorf)
- Results (Felsch et al., *BMC-MRM* 2022):
  - No advantages in the case of 2 studies
  - More power than HKSJ in the case of 3-4 studies



Consideration of inclusion of the BBM in the procedure described before

## Bayesian meta-analysis

- Required: Slightly informative prior for  $\tau$
- Good compromise between DSL und HKSJ
- IQWiG-project in collaboration with Tim Friede and Christian Röver (Göttingen):
  - Derivation of empirical priors for  $\tau$  from meta-analyses of IQWiG reports (see "*A Day with ... SMG*" 11.05.2021: <https://training.cochrane.org/learning-events/learning-live/day/day-smg>)
  - Currently: Estimation of empirical priors for  $\tau$  by means of the hierarchical Bayes model according to Röver et al. (*Stat. Med.* 2023, under review)
  - Manuscript in preparation with suggestion of priors for  $\tau$  for the effect measures RR, OR, HR, SMD (suitable for HTA) (Lilienthal et al., 2023, work in progress)

Evidence synthesis in the case of very few studies:

- Too large, unexplained heterogeneity: **QS**
- 2 studies:  
Standard model **FEM** (IV or MH)
- 3-4 studies:
  - **REM** with HKSJ or HKSJ-VC (if HKSJ yields useful information )
  - **QS** (if HKSJ yields no useful information or when DSL stat. sign.)
- 5 studies or more: REM with HKSJ or HKSJ-VC
- Future: BBM and Bayes (with informative prior for  $\tau$ )

# Conclusion

- No satisfactory universal standard method is currently available to perform meta-analyses in the case of very few studies
- Additional approaches (beta-binomial model, Bayes) are under consideration
- The procedure currently used by IQWiG (combination of FEM, REM, QS) represents a feasible approach to perform evidence syntheses with very few studies in practice

- Bender, R., Friede, T., Koch, A., Kuss, O., Schlattmann, P., Schwarzer, G. & Skipka, G. (2018): Methods for evidence synthesis in the case of very few studies. *Res. Syn. Methods* **9**, 382–392.
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